Algebra 2

Poudre School District

Pacing Overview

Semester One

Chapter 1: Linear Functions

10-11 days

HS.A.CED.A.2, HS.A.CED.A.3, HS.A.REI.C.6, HS.F.IF.C.9, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.LE.A.2, HS.S.ID.B.6a

Chapter 2: Quadratic Functions

7 days

HS.A.APR.B.3, HS.A.CED.A.2, HS.F.IF.B.4, HS.F.IF.B.6, HS.F.IF.C.7c, HS.F.IF.C.9, HS.F.BF.A.1a, HS.F.BF.B.3, HS.S.ID.B.6a

Chapter 3: Quadratic Equations and Complex Numbers (Part One)

8 days

HS.N.CN.A.1, HS.N.CN.A.2, HS.N.CN.C.7, HS.A.SSE.A.2, HS.A.REI.B.4b, HS.F.IF.C.8a

Chapter 4: Polynomial Functions

9-10 days

HS.N.CN.C.8, HS.N.CN.C.9, HS.A.SSE.A.2, HS.A.APR.A.1, HS.A.APR.B.2, HS.A.APR.B.3, HS.A.APR.C.4, HS.A.APR.C.5, HS.A.APR.D.6, HS.A.CED.A.2, HS.F.IF.B.4, HS.F.IF.C.7c, HS.F.BF.A.1a, HS.F.BF.B.3

Chapter 3: Quadratic Equations and Complex Numbers (Part Two)

3-4 days

HS.A.CED.A.1, HS.A.CED.A.3, HS.A.REI.C.7, HS.A.REI.D.11

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Semester Two

Chapter 5: Rational Exponents and Radical Functions

11-12 days

HS.N.RN.A.1, HS.N.RN.A.2, HS.A.CED.A.4, HS.A.REI.A.1, HS.A.REI.A.2, HS.F.IF.C.7b, HS.F.BF.A.1b, HS.F.BF.B.3, HS.F.BF.B.4a

Chapter 6: Exponential and Logarithmic Functions

13-14 days

HS.A.SSE.A.2, HS.A.SSE.B.3c, HS.A.CED.A.2, HS.A.REI.A.1, HS.F.IF.C.7e, HS.F.IF.C.8b, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.BF.B.4a, HS.F.LE.A.2, HS.F.LE.A.4, HS.F.LE.B.5

Chapter 7: Rational Functions

6 days

HS.A.APR.D.6, HS.A.APR.D.7, HS.A.CED.A.4, HS.A.REI.A.1, HS.A.REI.A.2, HS.F.BF.B.3

Chapter 10: Probability and Chapter 11: Data Analysis and Statistics

9-10 days

HS.A.APR.C.5, HS.S.ID.A.4, HS.S.CP.A.1, HS.S.CP.A.2, HS.S.CP.A.3, HS.S.CP.A.4, HS.S.CP.A.5, HS.S.CP.B.6, HS.S.CP.B.7, HS.S.CP.B.8, HS.S.CP.B.9

Chapter 8: Sequences and Series

Time Permitting

HS.A.SSE.B.4, HS.F.IF.A.3, HS.F.BF.A.1a, HS.F.BF.A.2, HS.F.LE.A.2

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Chapter 9: Trigonometric Ratios and Functions

Time Permitting

HS.A.CED.A.2, HS.F.IF.C.7e, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.TF.A.1, HS.F.TF.A.2, HS.F.TF.B.5, HS.F.TF.C.8, HS.F.TF.C.9

Chapter 11: Data Analysis and Statistics

Time Permitting

HS.S.ID.A.4, HS.S.IC.A.1, HS.S.IC.A.2, HS.S.IC.B.3, HS.S.IC.B.4, HS.S.IC.B.5, HS.S.IC.B.6

Review & Common Summative Assessment



Major Work of the Grade. Supporting Work of the Grade. Additional Work of the Grade.

Chapter 1: Learning Functions

10-11 days

HS.A.CED.A.2, HS.A.CED.A.3, HS.A.REI.C.6, HS.F.IF.C.9, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.LE.A.2, HS.S.ID.B.6a

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
1.1	Parent Functions and Transformations	Learning	HS.F.BF.B.3	2 days
1.2	Transformations of Linear and Absolute Value Functions	Learning	HS.F.BF.B.3	1 day
1.3	Modeling with Linear Functions	Learning	HS.A.CED.A.2, HS.F.IF.C.9, HS.F.BF.A.1a, HS.F.LE.A.2, HS.S.ID.B.6a	3 days
1.4	Solving Linear Systems	Learning	HS.A.CED.A.3, HS.A.REI.C.6	2 days

Total: 8 days

Additional Activities/Resources		
Name	Location	

Vocabulary				
correlation coefficient	horizontal shrink	horizontal stretch		
line of best fit	line of fit	linear equation in three variables		
ordered triple	parent function	reflection		
solution of a system of three linear equations	system of three linear equations	transformation		
translation	vertical shrink	vertical stretch		

	Standards
HS.A.CED.A.2	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
HS.A.CED.A.3	Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. <i>For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.</i>
HS.A.REI.C.6	Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.
HS.F.IF.C.9	Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
HS.F.LE.A.2	Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).

Standards (continued)		
HS.S.ID.B.6a	Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.	

Chapter 2: Quadratic Functions

7 days

HS.A.APR.B.3, HS.A.CED.A.2, HS.F.IF.B.4, HS.F.IF.B.6, HS.F.IF.C.7c, HS.F.IF.C.9, HS.F.BF.A.1a, HS.F.BF.B.3, HS.S.ID.B.6a

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
2.1	Transformations of Quadratic Functions	Learning	HS.F.IF.C.7c, HS.F.BF.B.3	1 day
2.2	Characteristics of Quadratic Functions	Learning	HS.F.IF.B.4, HS.F.IF.C.7c, HS.F.IF.C.9, HS.A.APR.B.3	1 day
2.4	Modeling with Quadratic Equations	Learning	HS.A.CED.A.2, HS.F.IF.B.6, HS.F.BF.A.1a, HS.S.ID.B.6a	3 days

Total: 5 days

Additional Activities/Resources		
Name	Location	

Vocabulary			
axis of symmetry	intercept form	maximum value	
minimum value	parabola	quadratic function	
standard form	vertex form	vertex of a parabola	

	Standards
HS.A.APR.B.3	Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
HS.A.CED.A.2	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
HS.F.IF.B.4	For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. <i>Key features include: intercepts; intervals where the function</i> <i>is increasing, decreasing, positive, or negative; relative maximums and</i> <i>minimums; symmetries; end behavior; and periodicity.</i>
HS.F.IF.B.6	Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
HS.F.IF.C.7c	Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.
HS.F.IF.C.9	Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Standards (continued)		
HS.S.ID.B.6a	Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.	

Chapter 3: Quadratic Equations and Complex Numbers (Part One)

8 days

HS.N.CN.A.1, HS.N.CN.A.2, HS.N.CN.C.7, HS.A.SSE.A.2, HS.A.REI.B.4b, HS.F.IF.C.8a

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
3.1	Solving Quadratic Equations	Learning	HS.A.SSE.A.2, HS.A.REI.B.4b, HS.F.IF.C.8a	2 days
3.2	Complex Numbers	Learning	HS.N.CN.A.1, HS.N.CN.A.2, HS.N.CN.C.7, HS.A.REI.B.4b	1 day
3.3	Completing the Square	Learning	HS.N.CN.C.7, HS.A.REI.B.4b, HS.F.IF.C.8a	2 days
3.4	Using the Quadratic Formula	Learning	HS.N.CN.C.7, HS.A.REI.B.4b	1 day

Total: 6 days

Additional Activities/Resources		
Name	Location	

Vocabulary			
completing the square	complex number	discriminant	
imaginary number	imaginary unit <i>i</i>	pure imaginary number	
quadratic equation in one variable	quadratic Formula	root of an equation	
zero of a function			

Standards			
HS.N.CN.A.1	Know there is a complex number <i>i</i> such that $i^2 = -1$, and every complex number has the form $a + bi$ with <i>a</i> and <i>b</i> real.		
HS.N.CN.A.2	Use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.		
HS.N.CN.C.7	Solve quadratic equations with real coefficients that have complex solutions.		
HS.A.SSE.A.2	Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.		
HS.A.REI.B.4b	Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm bi$ for real numbers a and b .		
HS.F.IF.C.8a	Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.		

Chapter 4: Polynomial Functions

9-10 days

HS.A.APR.A.1, HS.A.APR.B.2, HS.A.APR.B.3, HS.A.APR.C.4, HS.A.APR.C.5, HS.A.APR.D.6, HS.A.CED.A.2, HS.F.IF.B.4, HS.F.IF.C.7c, HS.F.BF.A.1a, HS.F.BF.B.3

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
4.1	Graphing Polynomial Functions	Learning	HS.F.IF.B.4, HS.F.IF.C.7c	1 day
4.2	Adding, Subtracting, and Multiplying Polynomials	Learning	HS.A.APR.A.1, HS.A.APR.C.4, HS.A.APR.C.5	2 days
4.8	Analyzing Graphs of Polynomials Functions	Learning	HS.A.APR.B.3, HS.F.IF.B.4, HS.F.IF.C.7c, HS.F.BF.B.3	2 days
4.3	Dividing Polynomials	Learning	HS.A.APR.B.2, HS.A.APR.D.6	2 days

Total: 7 days

Additional Activities/Resources		
Name	Location	

Vocabulary			
end behavior	even function	local maximum	
local minimum	odd function	Pascal's Triangle	
polynomial	polynomial function	polynomial long division	
synthetic division			

Standards			
HS.A.APR.A.1	Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.		
HS.A.APR.B.2	Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number a , the remainder on division by $x - a$ is $p(a)$, so $p(a) = 0$ if and only if $(x - a)$ is a factor of $p(x)$.		
HS.A.APR.B.3	Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.		
HS.A.APR.C.4	Prove polynomial identities and use them to describe numerical relationships. For example, the polynomial identity $(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$ can be used to generate Pythagorean triples.		
HS.A.APR.C.5	Know and apply the Binomial Theorem for the expansion of $(x + y)^n$ in powers of x and y for a positive integer n, where x and y are any numbers, with coefficients determined for example by Pascal's Triangle.		
HS.A.APR.D.6	Rewrite simple rational expressions in different forms; write $a(x)/b(x)$ in the form $q(x) + r(x)/b(x)$, where $a(x)$, $b(x)$, $q(x)$, and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$, using inspection, long division, or, for the more complicated examples, a computer algebra system.		

	Standards (continued)
HS.A.CED.A.2	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
HS.F.IF.B.4	For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. <i>Key features include: intercepts; intervals where the function</i> <i>is increasing, decreasing, positive, or negative; relative maximums and</i> <i>minimums; symmetries; end behavior; and periodicity.</i>
HS.F.IF.C.7c	Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Chapter 3: Quadratic Equations and Complex Numbers (Part Two)

3-4 days

HS.A.CED.A.1, HS.A.CED.A.3, HS.A.REI.C.7, HS.A.REI.D.11

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
3.5	Solving Nonlinear Systems	Learning	HS.A.CED.A.3, HS.A.REI.C.7, HS.A.REI.D.11	1 day
3.6	Quadratic Inequalities	Learning	HS.A.CED.A.1, HS.A.CED.A.3	1 day

Total: 2 days

Additional Activities/Resources		
Name	Location	

Vocabulary			
quadratic inequality in one variable	quadratic inequality in two variables	system of nonlinear equations	

Standards		
HS.A.CED.A.1	Create equations and inequalities in one variable and use them to solve problems. <i>Include equations arising from linear and quadratic functions,</i> <i>and simple rational and exponential functions.</i>	
HS.A.CED.A.3	Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. <i>For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.</i>	
HS.A.REI.C.7	Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line $y = -3x$ and the circle $x^2 + y^2 = 3$.	
HS.A.REI.D.11	Explain why the x-coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.	

Chapter 5: Rational Exponents and Radical Functions

11-12 days

HS.N.RN.A.1, HS.N.RN.A.2, HS.A.CED.A.4, HS.A.REI.A.1, HS.A.REI.A.2, HS.F.IF.C.7b, HS.F.BF.A.1b, HS.F.BF.B.3, HS.F.BF.B.4a

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
5.1	n th Roots and Rational Exponents	Learning	HS.N.RN.A.1, HS.N.RN.A.2	2 days
5.2	Properties of Rational Exponents and Radicals	Learning	HS.N.RN.A.2	2 days
5.3	Graphing Radical Functions	Learning	HS.F.IF.C.7b, <mark>HS.F.BF.B.3</mark>	1 day
5.4	Solving Radical Equations and Inequalities	Learning	HS.A.REI.A.1, HS.A.REI.A.2	2 days
5.5	Performing Function Operations	Learning	HS.F.BF.A.1b	1 day
5.6	Inverse of a Function	Learning	HS.A.CED.A.4, <mark>HS.F.BF.B.4a</mark>	1 day

Total: 9 days

Additional Activities/Resources	
Name	Location

	Vocabulary	
conjugate	extraneous solutions	index of a radical
inverse functions	like radicals	$n^{\mathrm{th}} \operatorname{root} \operatorname{of} a$
radical equation	radical function	simplest form

	Standards
HS.N.RN.A.1	Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. For example, we define $5^{1/3}$ to be the cube root of 5 because we want $(5^{1/3})^3 = 5^{(1/3)3}$ to hold, so $(5^{1/3})^3$ must equal 5.
HS.N.RN.A.2	Rewrite expressions involving radicals and rational exponents using the properties of exponents.
HS.A.CED.A.4	Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. <i>For example, rearrange Ohm's law V</i> = <i>IR to highlight resistance R</i> .
HS.A.REI.A.1	Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
HS.A.REI.A.2	Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.
HS.F.IF.C.7b	Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
HS.F.BF.A.1b	Determine an explicit expression, a recursive process, or steps for calculation from a context.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
HS.F.BF.B.4a	Solve an equation of the form $f(x) = c$ for a simple function f that has an inverse and write an expression for the inverse. For example, $f(x) = 2 x^3$ or $f(x) = (x+1)/(x-1)$ for $x \neq 1$.

Chapter 6: Exponential and Logarithmic Functions

13-14 days

HS.A.SSE.A.2, HS.A.SSE.B.3c, HS.A.CED.A.2, HS.A.REI.A.1, HS.F.IF.C.7e, HS.F.IF.C.8b, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.BF.B.4a, HS.F.LE.A.2, HS.F.LE.A.4, HS.F.LE.B.5

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
6.1	Exponential Growth and Decay Functions	Learning	HS.A.SSE.B.3c, HS.F.IF.C.7e, HS.F.IF.C.8b, HS.F.LE.A.2, <mark>HS.F.LE.B.5</mark>	2 days
6.2	The Natural Base <i>e</i>	Learning	HS.F.IF.C.7e, <mark>HS.F.LE.B.5</mark>	2 days
6.3	Logarithms and Logarithmic Functions	Learning	HS.F.IF.C.7e, <mark>HS.F.BF.B.4a</mark> , HS.F.LE.A.4	2 days
6.4	Transformations of Exponential and Logarithmic Functions	Learning	HS.F.IF.C.7e, <mark>HS.F.BF.B.3</mark>	1 day
6.5	Properties of Logarithms	Learning	HS.A.SSE.A.2, HS.F.LE.A.4	1.5 days
6.6	Solving Exponential and Logarithmic Equations	Learning	HS.A.REI.A.1, HS.F.LE.A.4	2 days
6.7	Modeling with Exponential and Logarithmic Functions	Learning	HS.A.CED.A.2, HS.F.BF.A.1a, HS.F.LE.A.2	0.5 day

Total: 11 days

Additional Activities/Resources	
Name	Location

	Vocabulary	
asymptote	common logarithm	decay factor
exponential decay function	exponential equations	exponential function
exponential growth function	growth factor	logarithm of <i>y</i> with base <i>b</i> function
logarithmic equations	natural base <i>e</i>	natural logarithm

Standards	
HS.A.SSE.A.2	Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.
HS.A.SSE.B.3c	Use the properties of exponents to transform expressions for exponential functions. For example the expression 1.15^t can be rewritten as $(1.15^{1/12})^{12t} \approx 1.012^{12t}$ to reveal the approximate equivalent monthly interest rate if the annual rate is 15%.
HS.A.CED.A.2	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
HS.A.REI.A.1	Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
HS.F.IF.C.7e	Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
HS.F.IF.C.8b	Use the properties of exponents to interpret expressions for exponential functions. For example, identify percent rate of change in functions such as $y = (1.02)^t$, $y = (0.97)^t$, $y = (1.01)12^t$, $y = (1.2)^t/10$, and classify them as representing exponential growth or decay.
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Standards (continued)	
HS.F.BF.B.4a	Solve an equation of the form $f(x) = c$ for a simple function f that has an inverse and write an expression for the inverse. For example, $f(x) = 2 x^3$ or $f(x) = (x+1)/(x-1)$ for $x \neq 1$.
HS.F.LE.A.2	Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).
HS.F.LE.A.4	For exponential models, express as a logarithm the solution to $ab^{ct} = d$ where a, c , and d are numbers and the base b is 2, 10, or e ; evaluate the logarithm using technology.
HS.F.LE.B.5	Interpret the parameters in a linear or exponential function in terms of a context.

Chapter 7: Rational Functions

6 days

HS.A.APR.D.6, HS.A.APR.D.7, HS.A.CED.A.4, HS.A.REI.A.1, HS.A.REI.A.2, HS.F.BF.B.3

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
7.2	Graphing Rational Functions	Learning	HS.A.APR.D.6, HS.F.BF.B.3	optional
7.3	Multiplying and Dividing Rational Expressions	Learning	HS.A.APR.D.6, HS.A.APR.D.7	1 day
7.4	Adding and Subtracting Rational Expressions	Learning	HS.A.APR.D.6, HS.A.APR.D.7	1.5 days
7.5	Solving Rational Equations	Learning	HS.A.CED.A.4, HS.A.REI.A.1, HS.A.REI.A.2	1.5 days

Total: 4 days

Additional Activities/Resources	
Name	Location

	Vocabulary	
complex fraction	cross multiplying	rational expression
rational function	simplified form of a rational expression	

	Standards
HS.A.APR.D.6	Rewrite simple rational expressions in different forms; write $a(x)/b(x)$ in the form $q(x) + r(x)/b(x)$, where $a(x)$, $b(x)$, $q(x)$, and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$, using inspection, long division, or, for the more complicated examples, a computer algebra system.
HS.A.APR.D.7	Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.
HS.A.CED.A.4	Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law $V = IR$ to highlight resistance R .
HS.A.REI.A.1	Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
HS.A.REI.A.2	Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Chapter 10: Probability and Chapter 11: Data Analysis and Statistics

9-10 days

HS.A.APR.C.5, HS.S.ID.A.4, HS.S.CP.A.1, HS.S.CP.A.2, HS.S.CP.A.3, HS.S.CP.A.4, HS.S.CP.A.5, HS.S.CP.B.6, HS.S.CP.B.7, HS.S.CP.B.8, HS.S.CP.B.9

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Cł	napter 10: Pr	obability	
	Chapter Opener/Mathematical Practices			
10.1	Sample Spaces and Probability	Learning	HS.S.CP.A.1	1 day
10.2	Independent and Dependent Events	Learning	HS.S.CP.A.1, HS.S.CP.A.2, HS.S.CP.A.3, HS.S.CP.A.5, HS.S.CP.B.6, HS.S.CP.B.8	0.5 day
10.3	Two-Way Tables and Probability	Learning	HS.S.CP.A.4, HS.S.CP.A.5	0.5 day
10.4	Probability of Disjoint and Overlapping Events	Learning	HS.S.CP.A.1, HS.S.CP.B.7	1 day
10.5	Permutations and Combinations	Learning	HS.A.APR.C.5, HS.S.CP.B.9	1.5 days
10.6	Binomial Distributions	Learning	HS.S.CP.B.9	1.5 days
Chapter 11: Data Analysis and Statistics				
11.1	Using Normal Distributions	Learning	HS.S.ID.A.4	1 day

Total: 7 days

Additional Activities/Resources			
Name	Location		

Vocabulary				
binomial distribution	binomial experiment	Binomial Theorem		
combination	compound event	conditional probability		
conditional relative frequency	dependent events	disjoint		
event	experimental probability	geometric probability		
independent events	join frequency	joint relative frequency		
marginal frequency	marginal relative frequency	mutually exclusive events		
<i>n</i> factorial	normal curve	normal distribution		
outcome	overlapping events	permutation		
probability distribution	probability of an event	probability experiment		
random variable	sample space	standard normal distribution		
theoretical probability	two-way table	z-score		

Standards		
HS.A.APR.C.5	Know and apply the Binomial Theorem for the expansion of $(x + y)^n$ in powers of <i>x</i> and <i>y</i> for a positive integer <i>n</i> , where <i>x</i> and <i>y</i> are any numbers, with coefficients determined for example by Pascal's Triangle.	
HS.S.ID.A.4	Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate populate percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve.	
HS.S.CP.A.1	Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").	
HS.S.CP.A.2	Understand that two events <i>A</i> and <i>B</i> are independent if the probability of <i>A</i> and <i>B</i> occurring together is the product of their probabilities, and use this characterization to determine if they are independent.	
HS.S.CP.A.3	Understand the conditional probability of <i>A</i> given <i>B</i> as $P(A \text{ and } B)/P(B)$, and interpret independence of <i>A</i> and <i>B</i> as saying that the conditional probability of <i>A</i> given <i>B</i> is the same as the probability of <i>A</i> , and the conditional probability of <i>B</i> given <i>A</i> is the same as the probability of <i>B</i> .	

	Standards (continued)
HS.S.CP.A.4	Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. <i>For example, collect data from a</i> <i>random sample of students in your school on their favorite subject among</i> <i>math, science, and English. Estimate the probability that a randomly</i> <i>selected student from your school will favor science given that the student is</i> <i>in tenth grade. Do the same for other subjects and compare the results.</i>
HS.S.CP.A.5	Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. <i>For example,</i> <i>compare the chance of having lung cancer if you are a smoker with the</i> <i>chance of being a smoker if you have lung cancer.</i>
HS.S.CP.B.6	Find the conditional probability of <i>A</i> given <i>B</i> as the fraction of <i>B</i> 's outcomes that also belong to <i>A</i> , and interpret the answer in terms of the model.
HS.S.CP.B.7	Apply the Addition Rule, $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$, and interpret the answer in terms of the model.
HS.S.CP.B.8	Apply the general Multiplication Rule in a uniform probability model, $P(A and B) = P(A)P(B A) = P(B)P(A B)$, and interpret the answer in terms of the model.
HS.S.CP.B.9	Use permutations and combinations to compute probabilities of compound events and solve problems.

Chapter 8: Sequences and Series

Time Permitting

HS.A.SSE.B.4, HS.F.IF.A.3, HS.F.BF.A.1a, HS.F.BF.A.2, HS.F.LE.A.2

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
8.1	Defining and Using Sequences and Series	Learning	HS.F.IF.A.3	0.5 day
8.2	Analyzing Arithmetic Sequences and Series	Learning	HS.F.IF.A.3, HS.F.BF.A.2, HS.F.LE.A.2	1 day
8.3	Analyzing Geometric Sequences and Series	Learning	HS.A.SSE.B.4, HS.F.IF.A.3, HS.F.BF.A.2, HS.F.LE.A.2	1 day
8.4	Finding Sums of Infinite Geometric Series	Learning	HS.A.SSE.B.4	0.5 day
8.5	Using Recursive Rules with Sequences	Learning	HS.F.IF.A.3, HS.F.BF.A.1a, HS.F.BF.A.2	1 day

Total: 4 days

Additional Activities/Resources			
Name	Location		

Vocabulary				
arithmetic sequence	arithmetic series	common difference common ratio		
explicit rule	geometric sequence	geometric series		
partial sum	recursive rule	sequence		
series	sigma notation	summation notation		
terms of a sequence				

Standards		
HS.A.SSE.B.4	Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems. <i>For example, calculate mortgage payments</i> .	
HS.F.IF.A.3	Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. For example, the Fibonacci sequence is defined recursively by $f(0) = f(1) = 1$, $f(n+1) = f(n) + f(n-1)$ for $n \ge 1$.	
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.	
HS.F.BF.A.2	Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.	
HS.F.LE.A.2	Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).	

Chapter 9: Trigonometric Ratios and Functions

Time Permitting

HS.A.CED.A.2, HS.F.IF.C.7e, HS.F.BF.A.1a, HS.F.BF.B.3, HS.F.TF.A.1, HS.F.TF.A.2, HS.F.TF.B.5, HS.F.TF.C.8, HS.F.TF.C.9

Chapter Summary				
Section	Title	Level of Learning	Standard(s)	Pacing
	Chapter Opener/Mathematical Practices			
9.1	Right Triangle Trigonometry	Preparing	HS.F.TF.A.1, <mark>HS.F.TF.A.2</mark> , HS.F.TF.B. <mark>5</mark> , <mark>HS.F.TF.C.8</mark>	1 day
9.2	Angles and Radian Measure	Learning	HS.F.TF.A.1	0.5 day
9.3	Trigonometric Functions of Any Angle	Learning	HS.F.TF.A.2	1 day
9.4	Graphing Sine and Cosine Functions	Learning	HS.F.IF.C.7e, HS.F.BF.B.3	1 day
9.5	Graphing Other Trigonometric Functions	Learning	HS.F.IF.C.7e, HS.F.BF.B.3	1 day
9.6	Modeling with Trigonometric Functions	Learning	HS.F.TF.B. <mark>5</mark> , HS.F.BF.A.1a, HS.A.CED.A.2	1 day
9.7	Using Trigonometric Identities	Learning	HS.F.TF.C.8	0.5 day
9.8	Using Sum and Difference Formulas	Learning	HS.F.TF.C.9	1 day

Total: 7 days

Additional Activities/Resources			
Name	Location		

Vocabulary				
amplitude	central angle	cosecant		
cosine	cotangent	conterminal		
cycle	fluency	initial side		
midline	period	periodic function		
phase shift	quadrantal angle	radian		
reference angle	secant	sector		
sine	sinusoid	standard position		
tangent	terminal side	trigonometric identity		
unit circle				

Standards		
HS.A.CED.A.2	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.	
HS.F.IF.C.7e	Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.	
HS.F.BF.A.1a	Determine an explicit expression, a recursive process, or steps for calculation from a context.	
HS.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.	
HS.F.TF.A.1	Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.	
HS.F.TF.A.2	Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.	
HS.F.TF.B.5	Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline.	
HS.F.TF.C.8	Prove the Pythagorean identity $\sin^2(\theta) + \cos^2(\theta) = 1$ and use it to find $\sin(\theta)$, $\cos(\theta)$, or $\tan(\theta)$ given $\sin(\theta)$, $\cos(\theta)$, or $\tan(\theta)$ and the quadrant of the angle.	

Standards (continued)	
HS.F.TF.C.9	Prove the addition and subtraction formulas for sine, cosine, and tangent and use them to solve problems.

Chapter 11: Data Analysis and Statistics

Time Permitting

HS.S.IC.A.1, HS.S.IC.A.2, HS.S.IC.B.3, HS.S.IC.B.4, HS.S.IC.B.5, HS.S.IC.B.6

Chapter Summary					
Section	Title	Level of Learning	Standard(s)	Pacing	
	Chapter Opener/Mathematical Practices				
11.2	Populations, Samples, and Hypotheses	Preparing Learning	HS.S.IC.A.1, HS.S.IC.A.2	0.5 day	
11.3	Collecting Data	Learning	HS.S.IC.A.1, HS.S.IC.B.3	1 day	
11.4	Experimental Design	Learning	HS.S.IC.A.1, HS.S.IC.B.3, HS.S.IC.B.6	1 day	
11.5	Making Inferences from Sample Surveys	Learning	HS.S.IC.A.2, HS.S.IC.B.4	1.5 days	
11.6	Making Inferences from Experiments	Learning	HS.S.IC.A.2, HS.S.IC.B.5	1 day	

Total: 6 days

Additional Activities/Resources		
Name	Location	

Vocabulary				
bias	biased question	biased sample		
cluster sample	control group	controlled experiment		
convenience sample	descriptive statistics	experiment		
hypothesis	inferential statistics	information design		
margin of error	observational study	parameter		
placebo	population	random sample		
randomization	randomized comparative experiment	replication		
sample	self-selected sample	simulation		
statistic	stratified sample	survey		
systematic sample	treatment group	unbiased sample		

Standards		
HS.S.IC.A.1	Understand statistics as a process for making inferences about population parameters based on a random sample from that population.	
HS.S.IC.A.2	Decide if a specified model is consistent with results from a given data- generating process, e.g., using simulation. <i>For example, a model says a</i> <i>spinning coin falls heads up with probability 0.5. Would a result of 5 tails in</i> <i>a row cause you to question the model</i> ?	
HS.S.IC.B.3	Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.	
HS.S.IC.B.4	Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling.	
HS.S.IC.B.5	Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant.	
HS.S.IC.B.6	Evaluate reports based on data.	